

Unit Two: Accelerated Motion; Acceleration due to gravity

- Acceleration occurs when an object speeds up, slows down or changes direction (a)
- Acceleration always agrees with net force
 - IF net force is zero; acceleration is zero
 - IF net force is positive, acceleration is positive
 - IF net force is negative, acceleration is negative

- To use head problem method
Solve smaller simple problems in stages



- Acceleration, velocity & displacement are vector quantities
- If initial velocity and acceleration don't agree in direction make sure they have opposite signs

- For projectiles in "free fall" the acceleration due to gravity is equal to gravitational field strength (g) = 9.81 m/s^2 downward

- If object is falling from rest displacement, final velocity & acceleration are all in the same direction so down can be assigned as positive

Approximation using $g = 10 \text{ m/s}^2$
 $d = (5 \text{ m/s}^2) t^2$ $v_f = (10 \text{ m/s}^2) t$

$$t = \sqrt{\frac{2d}{10 \text{ m/s}^2}}$$

a	t	d	v_f
10 m/s^2	1s	5m	10 m/s
$\frac{10}{2} \text{ m/s}^2$	2s	20m	20 m/s
	3s	45m	30 m/s
	4s	80m	40 m/s
	5s	125m	50 m/s
	6s	180m	60 m/s
	7s		

For
 • 1s $d = 5\text{m}$
 • 2s $d = 20\text{m}$

Equation, Variables, Units

v_i = initial velocity (speed)
 v_f = final velocity (speed) m/s
 $\bar{v}$ = average velocity (speed)
 Δv = Change in velocity (speed)
 a = acceleration (m/s^2)
 d = distance / displacement (m)
 t = time (s)

$$\bar{v} = \frac{v_i + v_f}{2} \quad \Delta v = v_f - v_i \quad a = \frac{\Delta v}{t}$$

When $v_i = 0$

$$v_f = v_i + at \quad v_f = at$$

$$v_f^2 = v_i^2 + 2ad \quad v_f^2 = 2ad$$

$$d = v_i t + \frac{1}{2} at^2 \quad d = \frac{1}{2} at^2$$

$$t = \sqrt{\frac{2d}{a}}$$

Graphs



$d = \frac{1}{2} at^2$
 d & t show direct square relationship
 $v_f = at$
 v & t show direct relationship
 acceleration is a constant non-zero
 $a = \frac{\Delta v}{t}$
 distance is area under $v(t)$
 Note if $d \propto t^2$
 $t \propto \sqrt{d}$
 $t = \sqrt{\frac{2d}{a}}$

Unit Two (continued): Projectiles in 1 and 2 dimensions

For projectiles launched upward remember the following rules

- launch velocity equal and opposite landing velocity
- acceleration is 9.8 m/s^2 downward for the entire time of flight
- The high point occurs at $\frac{1}{2}$ the total time of flight
- Speed at the high point is zero
- distance up equals distance down, overall displacement is zero

Flight can be divided into parts

$\frac{1}{2}$ Flight (up)

$a = -9.8 \text{ m/s}^2$

$v_f = 0$ at top

$v_i = \text{launch } v$

whole flight

$a = -9.8$

$v_i = \text{launch } v$

$v_f = \text{landing } v$

For Horizontal Projectiles

Vertical motion follows free fall $g = 9.8 \text{ m/s}^2$

Horizontal motion is in equilibrium. The horizontal velocity of a projectile does not change as the object falls

dx	v_x	+
dy	v_y	$\sqrt{v_x^2 + v_y^2}$
dx	v_x	dx
dy	v_y	dy

time in x equals time in y

For Projectiles launched at an angle

Gravity only acts on the vertical axis

mix of object launched upward with forward constant velocity

Break initial velocity into v_{ix} & v_{iy} using $v_{ix} = v_i \cos \theta$ $v_{iy} = v_i \sin \theta$

dx	v_{ix}	+
dy	v_{iy}	$\sqrt{v_{ix}^2 + v_{iy}^2}$
dx	v_{ix}	dx
dy	v_{iy}	dy

The maximum range for a projectile launched at an angle is 45° . Objects will land in the same location if launched at angles equal difference from 45° i.e. 30° & 60° ; 40° & 50°

Equations

For $\frac{1}{2}$ time of flight $t = \sqrt{\frac{2dy}{g}}$ $t = \frac{dv}{a}$

For object launched upward (vertical axis)

total flight $t = \frac{2v_{iy}}{g}$

$\Delta v = v_f - v_i$ ($v_f = -v_i$)

$\Delta v = -2v_{iy}$

$g = -9.8 \text{ m/s}^2$

$v_f = v_{iy} + g t$

$(v_f)^2 = (v_{iy})^2 + 2 a dy$

$dy = (v_{iy} t) + \frac{1}{2} g t^2$

Horizontal Motion

$dx = v_x t$



t is the same in x & y

$v_{ix} = v_i \cos \theta$

$\theta = \tan^{-1}(\frac{v_{iy}}{v_{ix}})$

45° launch greatest range

Highest angle is greatest time of flight

Graphs

For projectiles launched upward



For Horizontal projectiles

